

Each bound state can at most contain a pair of electrons with anti-parallel spins, and the number of these bound states is  $\frac{N}{2}$ . When  $T=0$ , all the bound states are filled up and there are no free electrons. At low temperatures, some electrons are excited ~~also~~ into the conduction band.

$$(a) \quad D(\epsilon) = \frac{4\pi}{(2\pi\hbar)^3} (2m)^{3/2} \sqrt{\epsilon}$$

(b, c) The problem is the same as I.4.

where  $N_0 = \frac{N}{2}$  and  $E_d = \epsilon_0$

$$N_f = \sqrt{N} \frac{2 \left( \frac{2\pi m T}{(2\pi\hbar)^3} \right)^{3/2}}{\left( \frac{2\pi\hbar}{2\pi\hbar} \right)^3} e^{-\frac{E_d}{2T}}$$

$$\mu = \frac{T}{2} \ln \left[ \frac{N}{2 \left( \frac{2\pi m T}{(2\pi\hbar)^3} \right)^{3/2}} \right] - \frac{E_d}{2}$$